

A quick trip through the text book shows that during our work in chapters 1, 3 and 4 that we have discussed the following:

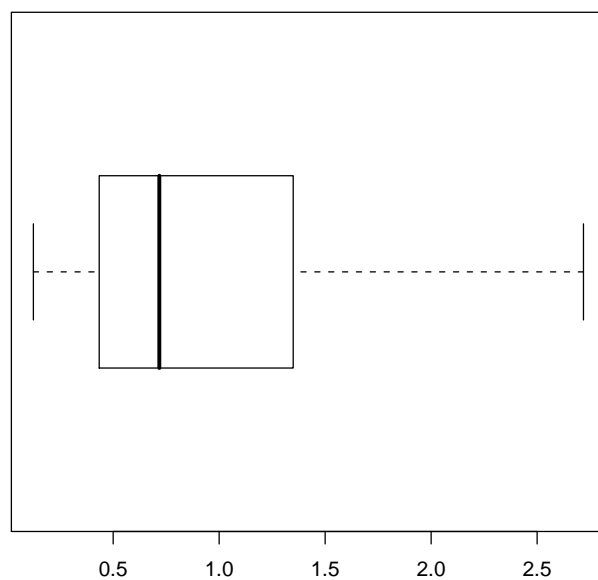
- types of variables: categorical, quantitative;
- center, spread, shape
- stemplot
- histogram
- boxplot
- density plot
- modes, symmetry, skew
- outliers (suspected outliers $1.5IQR$)
- mean, median
- quartiles, IQR, standard deviation
- five-number summary
- effect of linear transformation
- normal: rules of thumb, z-scores, standard normal, inverse CDF, qqplot
- lurking variables, confounding variables,
- Causation; common response, confounding (Ch. 2, p. 174)
- types of experiments
- comparative experiment
- placebo effect
- bias: lack of realism
- randomization
- randomized comparative experiment
- double blind, completely randomized
- matched pairs design
- block design
- population; sample

- statistic; parameter
- samples, SRS, stratified, multistage
- bias: response bias, wording of questions, lack of realism, ...
- sampling variability (Margin of Error)
- sampling distribution: center, spread, shape
- sample space, outcome, event, random variable
- rules of probability
- equally likely probabilities
- $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$
- independence
- conditional probability: $P(A | B) = P(A \text{ and } B) / P(B)$
- distribution of a discrete random variable X : $P(X = k) = \dots$
- mean of a discrete random variable. Expectation, $E(X) = \mu = \sum kP(X = k)$
- variance and standard deviation of a discrete random variable. $\sigma^2 = \sum (k - \mu)^2 P(X = k)$.

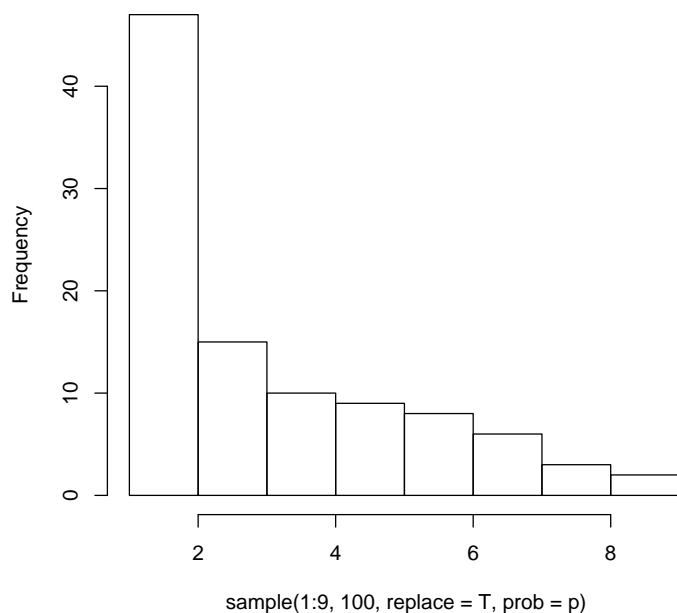
Here are some sample problems to work on during class. These are not meant to exhaust the full range of questions I may ask.

1. A 6-sided die has faces 1,1,2,3,5,8. Let X be the amount on one roll and Y the amount on 2 rolls of the die.
 - (a) Write down the probability distribution for X
 - (b) What is the expected value of X ?
 - (c) What is the expected value of Y ?
 - (d) The variance of X is $56/9$. What is the variance of Y ?
2. A teacher has 4 items from the snack machine: a candy bar, a pack of gum, a bag of chips and a pack of licorice. She hands out 2 of them.
 - (a) What is the probability the second one handed out is the pack of licorice?
 - (b) What is the probability the last one handed out is the pack of licorice?
 - (c) What is the probability the second one handed out is the pack of licorice, given that the first was a bag of chips?

3. A randomly chosen student has a 30% chance of being enrolled in a math class and a 35% chance of being enrolled in an English class. Suppose that the chance they are enrolled in both a math class *and* an English class is only 10%. What is the probability that a randomly chosen student is enrolled in either a math class *or* an English class?
4. If one tosses a fair coin 5 times a sequence results, say x_1, x_2, x_3, x_4, x_5 , where each x is either H or T .
 - (a) Find the probability of a sequence that produces 3 heads and 2 tails? (Does it matter which order the heads or tails are?)
 - (b) There are 10 different sequences that will produce 3 heads and 2 tails. Each of these outcomes is disjoint from the others. Use the last question to find the probability one will get 3 heads in 5 coin tosses.
 - (c) Explain, without doing any calculations, why this should be the same probability as getting 2 heads in 5 coin tosses *if* the coin is fair.
5. Recalling the rules of thumb for a normal, if math SAT scores for CSI students are normally distributed with a mean of 500 and standard deviation of 100, find the probability a randomly chosen student has an SAT score exceeding 600? Between 500 and 700?
6. Imagine that when 100 dice are rolled, the sum has a normal distribution with a mean of 350 and standard deviation of 17.
 - (a) Find the probability that in a given roll of 100 dice the sum is more than 370?
 - (b) Find a range of values centered around 350 for which 90% of the rolls (on average) will be in this interval. (You need to find the 5th and 95th percentiles)
7. A data set consists of values 1,1,2,3,4,5,8,15.
 - (a) What is n
 - (b) What is \bar{x} ?
 - (c) What is s
 - (d) What is the median?
 - (e) What is the IQR
8. A boxplot of a data set is shown. Based on this identify
 - (a) the median
 - (b) The IQR
 - (c) The max.
 - (d) Will the mean or median be greater? Why



Benford's law?



9.

A statistics teacher scrupulously records the first digit of each of receipts they receive. A histogram is shown.

(a) Is this data set skewed? symmetric? neither?

- (b) Is this data set unimodal, bimodal, multimodal?
- (c) Estimate the mean value for this data set.
- (d) there is something funny about this graphic in terms of representing the data.
Can you tell what it is?

10. Which of these data sets appears to be normally distributed?

