

Name: \_\_\_\_\_

1. Find the equation of the line that passes through the points  $(-1, 4)$  and  $(2, 10)$ . Give your answer as an equation in slope-intercept form (i.e., as  $y = mx + b$ ).

**Solution:** The slope is

$$m = \frac{10 - 4}{2 - (-1)} = 2.$$

In point-slope form, the equation is

$$y - 4 = 2(x + 1).$$

Rewriting this in slope-intercept form, we get

$$y = 2x + 6.$$

2. Expand  $(2x + 1)^2(x - 1)$  as a cubic polynomial, i.e., a polynomial of the form  $ax^3 + bx^2 + cx + d$  for constants  $a, b, c, d$ .

**Solution:**

$$\begin{aligned}(2x + 1)^2(x - 1) &= (4x^2 + 4x + 1)(x - 1) = 4x^3 + 4x^2 + x - 4x^2 - 4x - 1 \\ &= 4x^3 - 3x - 1.\end{aligned}$$

3. Find all solutions to  $x - \frac{7}{x} = 3$ . **Please note:**

- Give exact answers, not approximations.
- As you solve the problem, write down equations one after the other on the page, not scattered all around.
- Do not cross out or write on top of any equation; do not draw arrows that don't have any mathematical meaning.

**Solution:** Multiply both sides of the equation by  $x$  (we know that  $x \neq 0$ ):

$$x^2 - 7 = 3x.$$

Rewrite this as

$$x^2 - 3x - 7.$$

This doesn't factor, so we apply the quadratic formula to get

$$x = \frac{3 \pm \sqrt{9 + 4(7)}}{2} = \frac{3 \pm \sqrt{37}}{2}.$$