$$y'' + 12y' + 40y = \delta(t); \ y(0) = 0, \ y'(0) = 0$$

2. Solve the the following initial value problem:

$$y'' + 144y = \delta(t); \ y(0) = 0, \ y'(0) = 0$$

- 3. What is a convolution of two functions? What is the Laplace transform of a convolution product? (ie What is $\mathcal{L}[f*g]$)?
- 4. Compute the following convolution products:
 - (a) $e^{-3t} * e^{2t}$
 - (b) $H(t) * \cos 3t$
 - (c) $t * t^2$
- 5. Find the inverse Laplace transform of the following:
 - (a) $T(s) = \left(\frac{1}{s+3}\right) \left(\frac{1}{s-2}\right)$
 - (b) $T(s) = \left(\frac{1}{s}\right) \left(\frac{s}{s^2+9}\right)$

What is the connection to the results of Question 1?

- 6. Use the convolution theorem to find the inverse transforms of the following in terms of an integral. Do the integration if you can.
 - (a)

$$T(s) = \left(\frac{4}{s+4}\right) \left(\frac{1}{s-6}\right)$$

(b)

$$T(s) = \frac{3}{s(s^2 + 16)}$$

7. Use the convolution theorem to write the solution to the following IVP in terms of an integral FOR ANY f(t)

$$y'' + 6y' + 5y = f(t); \ y(0) = 0, \ y'(0) = 0$$

Use this general solution to find y(t) when $f(t) = e^{-2t}$.