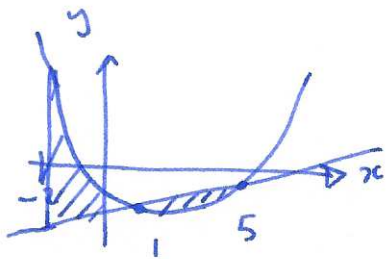


Examples • find area between graphs $f(x) = x^2 - 5x - 7$ on $[-2, 5]$ ⑦
and $g(x) = x - 12$

draw picture:



← need to break into two integrals

intersection points: $x^2 - 5x - 7 = x - 12$

$$x^2 - 6x + 5 = 0$$

$$(x-5)(x-1) = 0.$$

• find area of region bounded by $y = \frac{1}{x^2}$, $y = x$, $y = 12x$

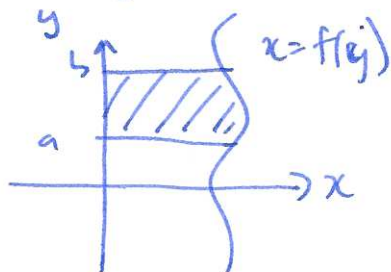
draw picture:



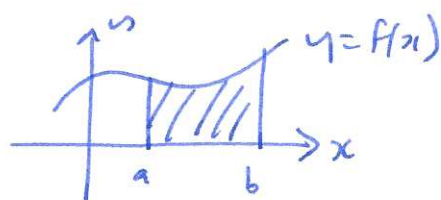
← need to break into two integrals

Integration along y-axis recall:

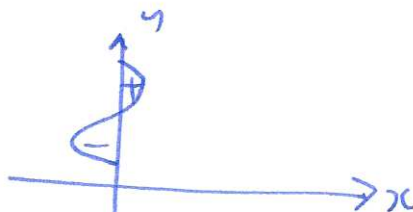
$$\int_a^b f(y) dy$$



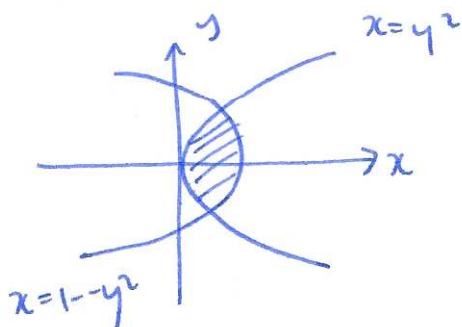
$$\int_a^b f(x) dx$$



signed area:



Example find area between the curves $x = y^2$ and $x = 1 - y^2$



intersection points

$$\int_{-1/\sqrt{2}}^{+1/\sqrt{2}} (1 - y^2 - y^2) dy$$

$$y^2 = 1 - y^2 \quad 2y^2 = 1 \quad y = \pm \frac{1}{\sqrt{2}}$$

§6.2 Volume, average value

recall: volume of cylinder is Ah



A = area of base

Fact: this works for cylinders of any base shape:

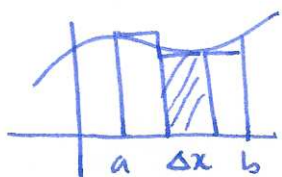


$$V = Ah$$

suppose shape is not a cylinder: can approximate by horizontal slices



recall:



← can approximate area under curve by rectangles of width Δx