

## §6.3 Use and abuse of tests

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- don't just say significant/not significant, report p-value.
- in large data sets, often find small statistically significant correlations, but not of much practical significance
- bad data sets not useful
- garden of forking paths.

## §6.4 Power and inference

$H_0$  null hypotheses.

$H_a$  alternate hypothesis.

|                          |              | Population.               |                                     |
|--------------------------|--------------|---------------------------|-------------------------------------|
|                          |              | $H_0$ true                | $H_a$ true                          |
| decision based on sample | Reject $H_0$ | Type I error ( $\alpha$ ) | correct decision                    |
|                          | Accept $H_0$ | correct decision          | Type II error. $(1 - \text{power})$ |

choose  $\alpha$ : this means we reject  $H_0$  if  $H_0$  is true only  $\alpha$  amount of the time, i.e.  $\alpha$  is the probability we make a Type I error.

Q: what about type II: we accept (do not reject)  $H_0$  even though  $H_a$  is true?  
want this prob. to be as small as possible, say prob =  $1 - \text{power}$   
i.e. want power of test to be as large as possible.

Example 6.17: water quality: test for lead parts per billion  $N(\mu, \sigma)$   
(assume  $\sigma = 0.25$ ). EPA says limit is 15 ppb.

$$H_0: \mu = 15$$

$$H_a: \mu \neq 15 \text{ (two sided)}$$

$$\alpha = 0.01$$

sample: 15.84, 15.33, 15.58

$$\bar{x} = \frac{15.84 + 15.33 + 15.58}{3} = 15.58$$

$$\text{test statistic: } z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}} = \frac{15.58 - 15.00}{0.25/\sqrt{3}} = 4.02$$