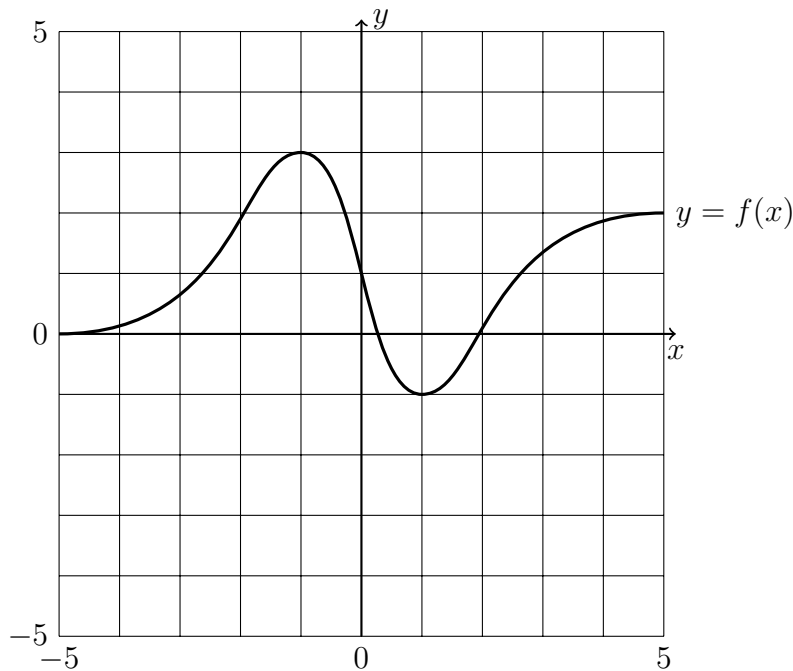


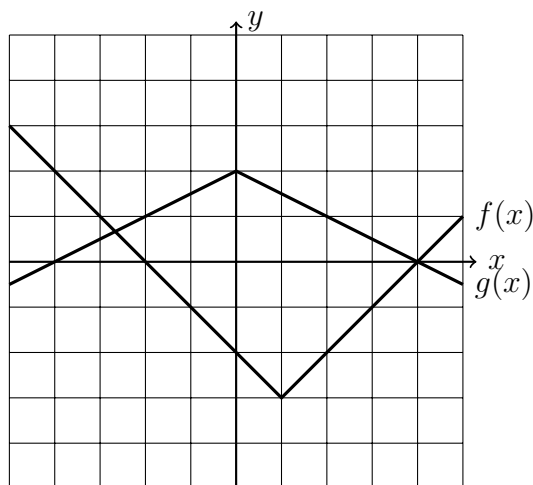
Math 231 Calculus 1 Fall 18 Sample Midterm 2

- (1) Consider the function $f(x)$ defined by the following graph.



- (a) Label all regions where $f'(x) < 0$.
 - (b) Label all regions where $f'(x) > 0$.
 - (c) Sketch a graph of $f'(x)$ on the figure.
 - (d) What is $\lim_{x \rightarrow \infty} f(x)$?
 - (e) What is $\lim_{x \rightarrow -\infty} f'(x)$?
- (2) Find the derivatives of the following functions
- (a) $x^3 e^{-4x^2}$
 - (b) $\frac{\sqrt{2x+1}}{3 - \sec(2x)}$
 - (c) x^{3x}
 - (d) $\ln(\tan(3x))$
 - (e) $\tan^{-1}(3/\sqrt[3]{x})$
 - (f) $\cos^{-1}(1 - 2x)$
- (3) Find the second derivatives of the functions above.

- (4) The graphs of the functions f and g are shown below.



- (a) Let $h(x) = f(x)g(x)$. Find $h'(2)$.
 - (b) Let $h(x) = f(g(x))$. Find $h'(-1)$.
- (5) Use implicit differentiation to find the tangent line to the hyperbola $4x^2 - 9y^2 = 7$ at the point $(2, -1)$.
 - (6) Find $\frac{dy}{dx}$ for the implicit function $x^2y + 2x^2y = -\cos(xy)$.
 - (7) You inflate a spherical balloon at a rate of 10cm^3 per second. How fast is the area of the balloon increasing when the radius is 10cm ?
 - (8) Use a linear approximation to estimate $\sqrt[3]{63}$. What is the percentage error?
 - (9) Find all the critical points for the function $f(x) = 2x^3 - 3x^2 - 36x + 4$. Use the first derivative test to identify them as local maxima or local minima.
 - (10) Find the absolute maximum and minimum of the function $f(x) = x^2 + 2x - 3$ on the interval $[-2, 2]$.