

$$1. \quad \cos^2 t + \sin^2 t = 1$$

$$\cos^2 t = 1 - \sin^2 t$$

$$\cos t = \pm \sqrt{1 - \sin^2 t}$$

$$\cos t = -\sqrt{1 - \sin^2 t}$$

MTH 130 Precalculus, Classwork 12/13

Fall 2014

(1) Write $\cos(t)$ in terms of $\sin(t)$ in Quadrant III.

(2) Write $\tan(t)$ in terms of $\cos(t)$ in Quadrant IV.

(3) If $\cos(t) = \frac{4}{5}$ and t is in Quadrant III, find the values of the other trig functions at t .

(4) Is $f(x) = x \sin^3(x)$ even, odd, or neither?

(5) Draw careful graphs of $y = \sin(x)$ and $y = 3 \sin(2x + \pi)$.

$$2. \quad \frac{\cos^2 t + \sin^2 t}{\cos^2 t} = \frac{1}{\cos^2 t}$$

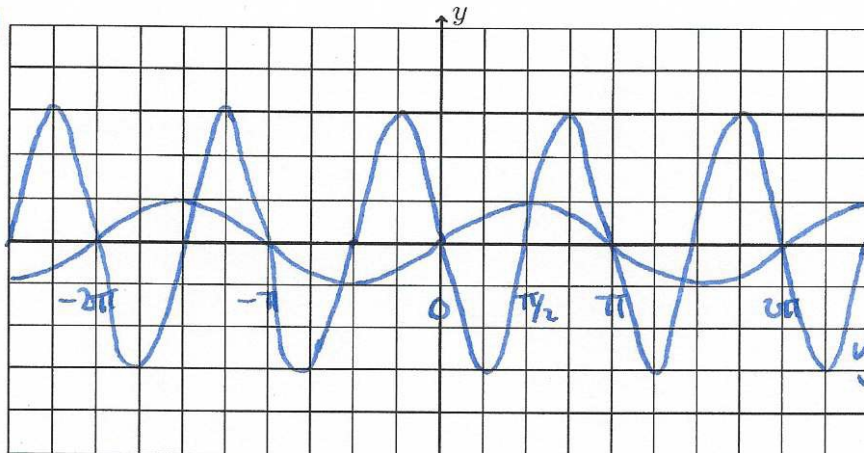
$$1 + \tan^2 t = \sec^2 t$$

$$\tan^2 t = \sec^2 t - 1$$

$$\tan t = \pm \sqrt{\sec^2 t - 1}$$

$$\tan t = -\sqrt{\sec^2 t - 1}$$

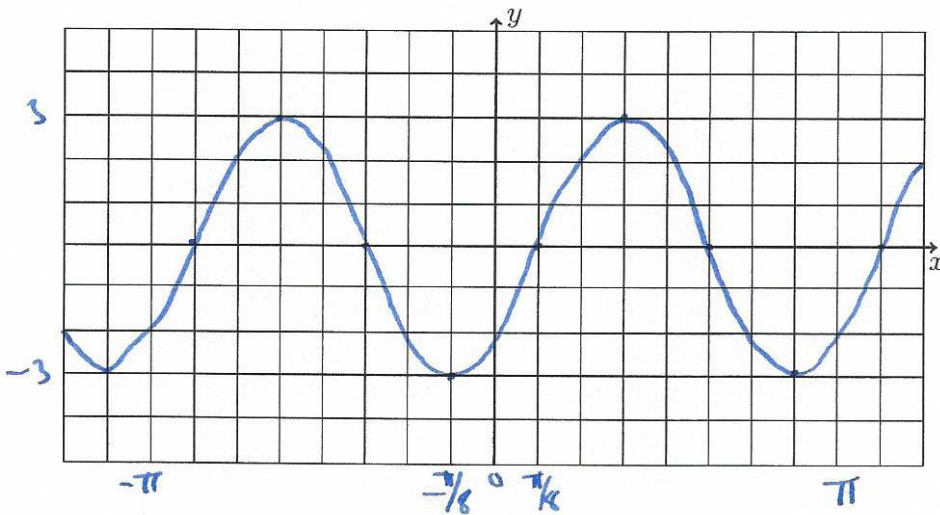
$$3 \sin\left(2\left(x - \left(-\frac{\pi}{2}\right)\right)\right)$$



$$y = \sin(x)$$

$$y = 3 \sin\left(2\left(x - \left(-\frac{\pi}{2}\right)\right)\right)$$

(6) Find the amplitude, frequency and phase shift for $y = -3 \cos(2x + \pi/4)$, and draw a careful graph of the function.



$$\text{amplitude} = 3$$

$$\text{frequency } \frac{2\pi}{2} = \pi$$

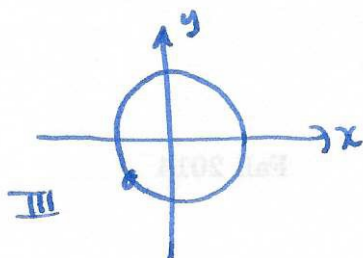
$$\text{period } 2$$

$$\text{frequency} = 2$$

$$-3 \cos\left(2\left(x - \left(\frac{\pi}{8}\right)\right)\right)$$

$$\text{phase shift } \frac{\pi}{8}$$

Q3



$$x^2 + y^2 = 1$$

$$\cos^2 t + \sin^2 t = 1$$

$$\left(-\frac{4}{5}\right)^2 + y^2 = 1$$

$$y^2 = 1 - \frac{16}{25} = \frac{25-16}{25} = \frac{9}{25}$$

$$y = \pm \frac{3}{5} \quad y = -\frac{3}{5}$$

$$\cos t = -\frac{4}{5}$$

$$\sin t = -\frac{3}{5}$$

$$\tan t = \frac{\sin t}{\cos t} = \frac{-3/5}{-4/5} = \frac{3}{4}$$

$$\sec t = \frac{1}{\cos t} = -\frac{5}{4}$$

$$\csc t = \frac{1}{\sin t} = -\frac{5}{3}$$

$$\cot(t) = \frac{1}{\tan t} = \frac{4}{3}$$

Q4

$$f(-x) = -x \sin^3(-x)$$

$$\sin(-x) = -\sin(x)$$

$$= -x (-\sin(x))^3$$

$$= -x \cdot -\sin^3(x) = x \sin^3(x) \quad \text{even.}$$

