

(1) Find formulas for the inverse function of the following functions.

(a) $\frac{1}{x+1}$

$$y = \frac{1}{x+1} \quad y(x+1) = 1 \quad xy + y = 1$$

$$xy = 1 - y \quad x = \frac{1-y}{y} \quad f^{-1}(x) = \frac{1-x}{x}$$

(b) $\frac{2x-3}{4-4x}$

$$y = \frac{2x-3}{4-4x} \quad y(4-4x) = 2x-3 \quad 4y - 4xy = 2x-3$$

$$4y+3 = 2x+4xy \quad 4y+3 = x(2+4y) \quad x = \frac{4y+3}{2+4y}$$

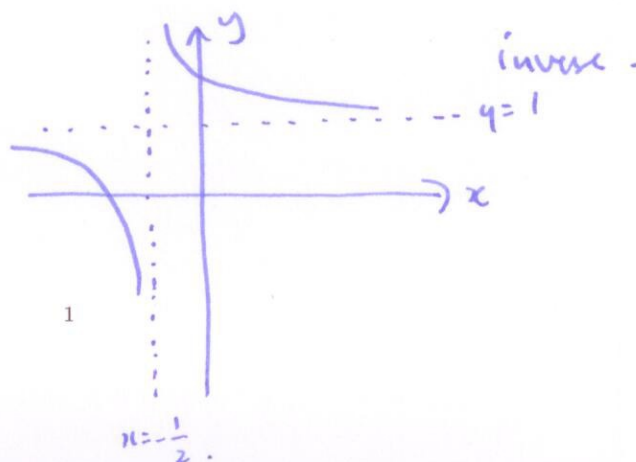
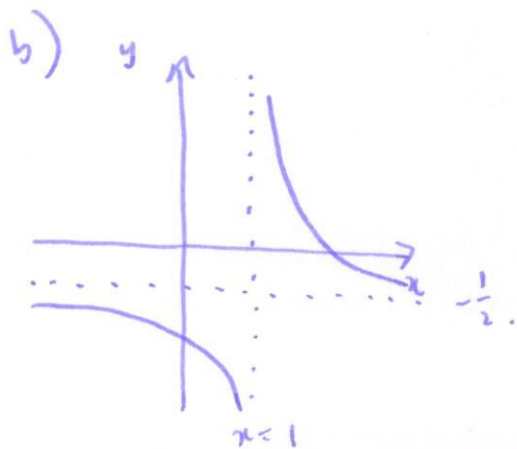
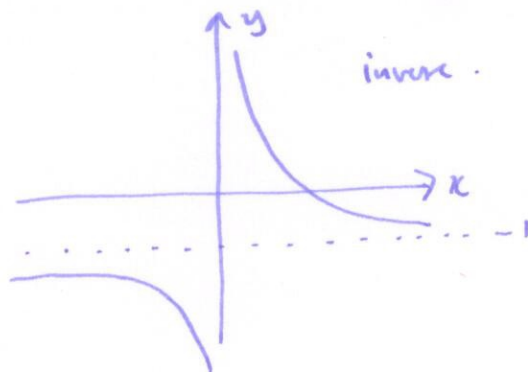
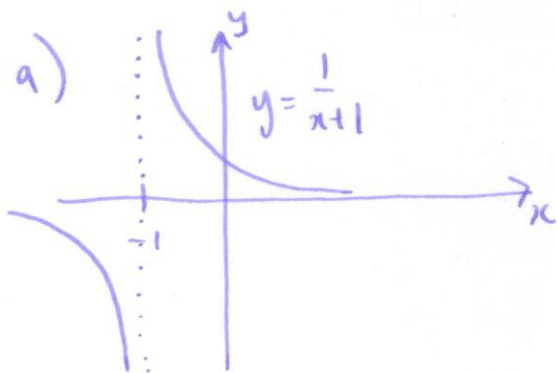
$$f^{-1}(x) = \frac{4x+3}{2+4x}$$

(c) $\sqrt{2x-1}$

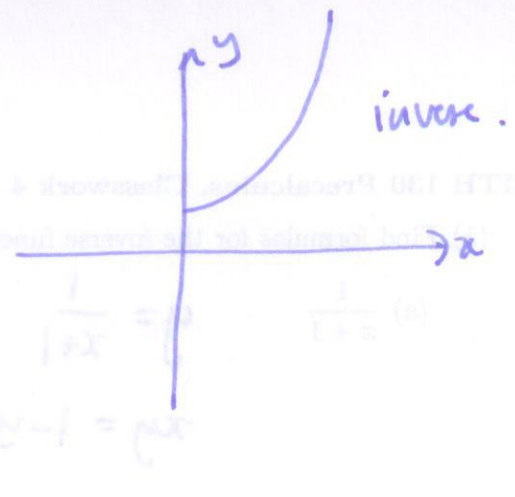
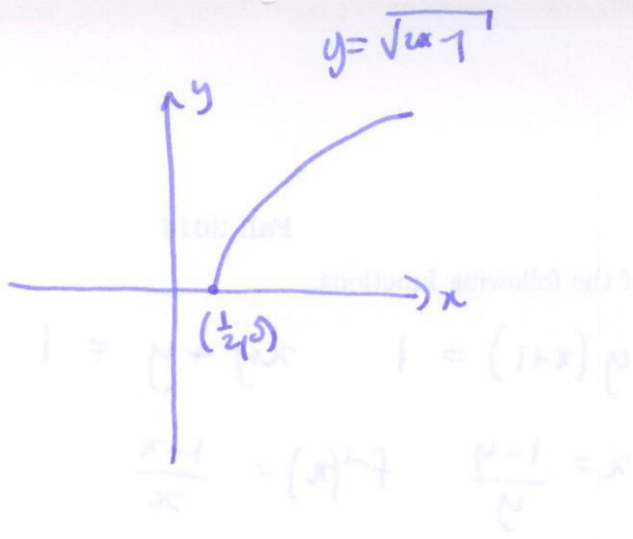
$$y = \sqrt{2x-1} \quad y^2 = 2x-1 \quad y^2+1 = 2x \quad x = \frac{1}{2}(y^2+1)$$

$$f^{-1}(x) = \frac{1}{2}(x^2+1)$$

(2) Sketch the graphs of the functions and their inverse functions.



c)



$$y = \sqrt{x-1} \Rightarrow y^2 = x-1 \Rightarrow x = y^2 + 1$$

$$f^{-1}(y) = y^2 + 1$$

$$y = \sqrt{x-1} \Rightarrow y^2 = x-1 \Rightarrow x = y^2 + 1$$

$$f^{-1}(y) = y^2 + 1$$

$$f^{-1}(x) = \frac{1}{2}(x+1)$$

$$f^{-1}(x) = \frac{1}{2}(x+1)$$

