Math 232 Calculus 2 Fall 12 Sample midterm 2

(1) Find
$$\int_{0}^{\pi/2} \sin^{3}(x) \cos^{2}(x) dx$$

(2) Find
$$\int \cos(3x) \cos(5x) dx.$$

(3) Find
$$\int \frac{x^{2}}{\sqrt{x^{2}+1}} dx.$$

(4) Find
$$\int \frac{x^{2}+11x}{(x-1)(x+1)^{2}} dx.$$

(5) Find
$$\int_0^\infty x \ln x \, dx$$
.

(6) Find
$$\int_0^\infty \frac{1}{4+x^2} \, dx.$$

- (7) Find the center of mass of the region above the x-axis and below the curve $y = x^2 4x$.
- (8) Find the degree three Taylor polynomial centered at x = 1 for the function $f(x) = \sqrt{2x+1}$.
- (9) Does the series $\sum_{n=1}^{\infty} \frac{\ln n}{n^3}$ converge or diverge?
- (10) Does the series $\sum_{n=1}^{\infty} \sin(\frac{1}{n})$ converge or diverge? (Hint: draw graph of $\sin(x)$ and think about the comparison test.)