## Math 229 Calculus Computer Lab Fall 11 Sample Final

• You may use only MATLAB during this exam. No calculators.

**Problem 1.** (10pts.) Use MATLAB to find all x (to three decimal places) where

$$4\cos(5x) = x^2 - 15$$

Give the answer, and write the MATLAB commands used to get your answer.

**Problem 2.** (10pts.) Let  $f(x) = \cos(2x) - 4x$ . Starting at  $x_0 = 1$ , apply Newton's method to find where f(x) = 0 to four decimal places. Write the iterations  $x_1, x_2, \ldots$  as many as needed.

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

**Problem 3.** (10pts.) Let  $f(x) = 4x^6 - 7x^2 + 4$ .

- (a) Write the commands to compute the roots of f(x) using the roots function in MATLAB.
- (b) How many real and complex roots are listed as the output of the roots function?
- (c) What are the real root(s) to <u>four</u> decimal places?

## **Problem 4.** (10pts.)

Find the minimum of  $f(x) = \left(4\sin(x+1) + \frac{2}{(x-\pi)^4}\right)$  on  $(0,\pi)$ . Write the x-value to <u>three</u> decimal places, and the final MATLAB commands you used to get your answer.

**Problem 5.** (20pts.) Let 
$$f(x) = \sqrt{3x} \sin\left(\frac{5}{\sqrt{x}}\right)$$
 for  $x > 0$ .

- (a) Write the m-file for the function f(x).
- (b) Compute  $f\left(\sqrt{7}\right)$  to <u>ten</u> decimal places. (Do not use scientific notation.)
- (c) Compute  $\lim_{x\to 0^+} f(x)$  to <u>four</u> decimal places. (Do not use scientific notation.)
- (d) Compute  $\lim_{x\to\infty} f(x)$  to <u>four</u> decimal places. (Do not use scientific notation.)
- (e) Find the x-value of the absolute minimum of f(x) to three decimal places.

**Problem 6.** (20pts.) Let 
$$f(x) = \tan(x/7) \cos(x-1)$$
.

- (a) Write the m-file for the function f(x).
- (b) Plot f(x) and its approximate derivative with h = 0.001, for  $0 \le x \le 2\pi$ . Find the x-coordinates of the following points (accurate to three decimal places):
  - (i) Points where f(x) = 0:
  - (ii) Points where f'(x) = 0:
  - (iii) Points where f''(x) = 0 (Recall, f''(x) is the first derivative of f'(x)):
  - (iv) Points where f(x) = f'(x):

**Problem 7.** (20pts.) Find the point P(x, y) on the curve  $y = e^{x/3}$  that is closest to the point Q(5,3).

- (a) What function d(x,y) gives the distance from P(x,y) on the curve to Q(5,3)?
- (b) Write the m-file for the function d(x) (depending only on x) that gives the distance from P(x, y) on the curve to Q(5, 3).
- (c) Using d(x) from part (b), what is diffuo for d'(x) with h = 0.001?
- (d) Plot diffuo for  $0 \le x \le 5$ . For which x is d'(x) = 0 (to <u>three</u> decimal places)?
- (e) What is P(x,y) on the curve? Give coordinates to three decimal places.
- (f) Why is this x-value a minimum for d(x)? Apply the first derivative test: How does the graph cross the x-axis?