April 30, 2014 Professor Ilya Kofman

NAME: $\qquad$

1. For the five statements below, fill in the chart with $\mathbf{A} \mathbf{S} \mathbf{N}$ in each space. $X 1$ : Two distinct points determine a unique line.
$X 2$ : Two distinct lines intersect in a unique point.
$X 3$ : For a line $\ell$ and point $Q$ off $\ell$, there exists a line parallel to $\ell$ through $Q$.
$X 4$ : For a line $\ell$ and point $Q$ off $\ell$, a unique line is parallel to $\ell$ through $Q$.
$X 5$ : If two triangles are similar then they are congruent.

|  | $X 1$ | $X 2$ | $X 3$ | $X 4$ | $X 5$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{R}^{2}$ |  |  |  |  |  |
| $S^{2}$ |  |  |  |  |  |
| $\mathbf{R} P^{2}$ |  |  |  |  |  |
| $\mathbf{H}^{2}$ |  |  |  |  |  |
| Taxicab |  |  |  |  |  |

2. Given two points $A, B$ in $S^{2}$, precisely describe an orientation-preserving isometry of $S^{2}$ that exchanges $A$ and $B$. Do the same for $\mathbf{H}^{2}$.
3. Draw a perspective view of a tiled floor with straightedge alone (at least nine rectangular tiles).
