

## Extra Problems for Quiz 1

Calculus III, MTH 233



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- Let  $\vec{a} = \langle 4, -3, -1 \rangle$  and  $\vec{b} = \langle -2, -3, 5 \rangle$ . Compute the following:  
(a)  $\vec{a} + \vec{b}$  (b)  $2\vec{a} - 3\vec{b}$  (c)  $\|\vec{a} + \vec{b}\|$   
(d)  $\vec{a} \cdot \vec{b}$  (e)  $\vec{a} \times \vec{b}$  (f)  $\text{proj}_{\vec{a}} \vec{b}$
  - Find the area of the triangle with vertices  $(1, 2, 3)$ ,  $(3, 1, 5)$  and  $(4, 5, 6)$ .
  - 3 points are collinear if they lie on the same line. Determine whether the points  $(1, 1, 2)$ ,  $(0, 1, 0)$  and  $(1, 2, 3)$  are collinear. (Hint: cross product)
  - 4 points are coplanar if they lie of the same plane. Determine whether the points  $(0, 2, 1)$ ,  $(0, 1, 0)$ ,  $(1, 1, 0)$  and  $(1, 2, 3)$  are coplanar. (Hint: scalar triple product)
  - Find the angle between the vectors  $\vec{a} = -4\vec{i} + 2\vec{j} + 3\vec{k}$  and  $\vec{b} = 2\vec{i} + \vec{j} + 5\vec{k}$ .
  - Find the angle that  $\vec{a}$  makes with the  $z$ -axis.
  - Find the angle between the planes  $y - z = 5$  and  $x - z = 7$ .
  - Find the equation of the plane passing through the points  $(1, 3, 2)$ ,  $(0, 3, 0)$  and  $(2, 4, 3)$ .
  - Find the equation of a plane passing through point  $(2, 1, 0)$  and parallel to the plane  $x - 2y + 5z = 3$ . Does this plane pass through the origin ?
  - Find the equation of a plane perpendicular to the line  $x = 2 + 3t$ ,  $y = -t$ ,  $z = -1 + t$  and passing through point  $(0, 1, -1)$ .
  - Identify the following surfaces using their traces in planes parallel to the co-ordinate planes.  
(a)  $9x^2 + 4y^2 = 2z^2$  (b)  $4x^2 + 4y^2 + z^2 = 16$  (c)  $4x^2 + 4y^2 - z^2 = 16$   
(d)  $9x^2 - 4y^2 = 72$  (e)  $z = 9x^2 - 4y^2$  (f)  $z = 9x^2 + 4y^2$