

Classwork 8

College Algebra and Trigonometry, MTH 123, Section 3260, Fall 2011
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Name: Solution

1. Find the inverse of the function $f(x) = \sqrt{3 - 4x}$.

$$\begin{aligned} y &= \sqrt{3 - 4x} \\ y^2 &= 3 - 4x \\ 4x &= 3 - y^2 \\ x &= \frac{3 - y^2}{4} \\ y &= \frac{3 - x^2}{4} \end{aligned}$$

*Switch
x & y*

$$f^{-1}(x) = \frac{3 - x^2}{4}$$

2. Find the inverse of the function $f(x) = \frac{1}{x-1}$.

$$\begin{aligned} y &= \frac{1}{x-1} \\ x-1 &= \frac{1}{y} \\ x &= \frac{1}{y} + 1 \\ y &= \frac{1}{x} + 1 \end{aligned}$$

$$f^{-1}(x) = \frac{1}{x} + 1$$

3. Find the inverse of the function $f(x) = \frac{1+3x}{5-2x}$.

$$\begin{aligned} y &= \frac{1+3x}{5-2x} \\ 5y - 2xy &= 1 + 3x \\ 5y - 1 &= 2xy + 3x \\ 5y - 1 &= x(2y + 3) \\ \frac{5y - 1}{2y + 3} &= x \end{aligned}$$

$$y = \frac{5x - 1}{2x + 3}$$

$$f^{-1}(x) = \frac{5x - 1}{2x + 3}$$