Date: March 15, 2006 Professor Ilya Kofman Justify answers and show all work for full credit. No calculators allowed.

NAME: _____

Problem 1. Compute the derivative of the following functions. Show all work!

(a) $f(x) = (x^2 + 3x)^9 \sqrt{x^3 - 5}$

(b)
$$f(x) = e^{\sin(x^2 - 1)}$$

(c)
$$f(x) = e^{-6x} \cos(2x)$$

(d)
$$f(x) = \frac{x^4}{10x^2 - 8}$$

(e)
$$f(x) = \ln(x^{\frac{3}{2}} + 5)$$

Problem 2. Let $f(x) = x^2 + 3x$. Use the definition of the derivative to find f'(1).

Problem 3. Compute using the definition of the derivative: $\lim_{h \to 0} \frac{\sqrt[3]{-8+h}+2}{h}$

Problem 4. A ball is thrown upward from 64 feet above the ground, with an initial velocity of 48 ft/sec.

(a) Find the velocity of the ball when it hits the ground.

(b) Find the maximum height of the ball.

Problem 5. Suppose x and y satisfy $x + x^2y + \cos y = 2$

(a) Find $\frac{dy}{dx}$ as a function of x and y.

(b) Find an equation of the tangent line to this graph at the point (1,0).

Problem 6. A paper cup has the shape of a cone with height 5 cm, and radius at the top 4 cm. Water leaks out of the cup at $3 \text{ m}\ell/\text{min}$. At what rate is the height of the water dropping when the cup still has 2 cm of water in it?

Draw a picture and indicate all quantities that you know and the ones you must find. [Hint: Choose the correct formula: $V = 4\pi r^2 h$, $V = \frac{1}{3}\pi r^2 h$, $V = \frac{4}{3}\pi r^2 h$]