Sample problems for Exam 1 for Math 233

This sample exam has many more questions than the actual exam will have.

- 1. Let $\vec{\mathbf{a}} = \langle 4, -3, -1 \rangle$ and $\vec{\mathbf{b}} = \langle -2, -3, 5 \rangle$. Find (a) $\vec{\mathbf{a}} + \vec{\mathbf{b}}$ (b) $2\vec{\mathbf{a}} 3\vec{\mathbf{b}}$ (c) $|\vec{\mathbf{a}}|$ (d) $|\vec{\mathbf{b}}|$ (e) $|\vec{\mathbf{a}} + \vec{\mathbf{b}}|$ (f) $\vec{\mathbf{a}} \cdot \vec{\mathbf{b}}$ (g) $\vec{\mathbf{a}} \times \vec{\mathbf{b}}$ (h) $\operatorname{proj}_{\vec{\mathbf{a}}} \vec{\mathbf{b}}$ (i) $\operatorname{proj}_{\vec{\mathbf{b}}} \vec{\mathbf{a}}$
- 2. Find the angle between the vectors $\vec{\mathbf{a}} = -4\vec{\mathbf{i}} + 2\vec{\mathbf{j}} + 3\vec{\mathbf{k}}$ and $\vec{\mathbf{b}} = 2\vec{\mathbf{i}} + \vec{\mathbf{j}} + 5\vec{\mathbf{k}}$. Find the angle that $\vec{\mathbf{a}}$ makes with the z-axis. (Note this is its ϕ in spherical coordinates.)
- 3. Express the vector $\vec{\mathbf{u}} = \langle 2, 4, 5 \rangle$ as a sum of vector $\vec{\mathbf{m}}$ parallel to $\vec{\mathbf{v}} = \langle 2, -1, -2 \rangle$, and a vector $\vec{\mathbf{n}}$ perpendicular to $\vec{\mathbf{v}}$.
- 4. Find the area of the triangle with vertices (1, 2, 3), (3, 1, 5) and (4, 5, 6).
- 5. Find the area of the parallelogram with vertices (-1, 2, 0), (1, 0, 1), (-2, 0, 0) and (0, -2, 1).
- 6. Find unit vectors perpendicular to the plane passing through the points (1, 3, 5), (3, -1, 2) and (4, 0, 1).
- 7. Find the parametric and symmetric equations of the line passing through the points (4, 5, 6) and (3, 2, 1).
- 8. Find the parametric and symmetric equations of the line at the intersection of the planes, 3x 3y 7z = -4 and x y + 2z = 3.
- 9. Find the equation of the plane passing through the points (1,3,2), (0,3,0) and (2,4,3).
- 10. Find the equation of a plane passing through point (2,1,0) and containing the line $\frac{x-3}{2} = y = \frac{-8-z}{1}$.
- 11. Find the equation of a plane perpendicular to the line x = 2 + 3t, y = -t, z = -1 + tand passing through point (0, 1, -1).
- 12. Determine whether the points (1, 1, 2), (0, 1, 0) and (1, 2, 3) are collinear.
- 13. Determine whether the points (0, 2, 1), (0, 1, 0), (1, 1, 0) and (1, 2, 3) are coplanar.
- 14. Find the equation of the plane perpendicular to the line x = 1 + 2t, y = -3 + 4t, z = -1 t and passing through the point (-1, -1, 5).
- 15. Find the distance between the parallel planes 3x + 3y 9z = 4 and x + y 3z = 1.
- 16. Describe and sketch the surface $z = x^2 4y^2$.
- 17. Describe and sketch the surface $x^2 y^2 z^2 4 = 0$.
- 18. Find the cylindrical and spherical coordinates for the point $P(\sqrt{3}, 1, 2\sqrt{3})$.
- 19. Describe and sketch the surface given in spherical coordinates by $\phi = \pi/3$. Find the equations in cylindrical and cartesian coordinates for this surface.